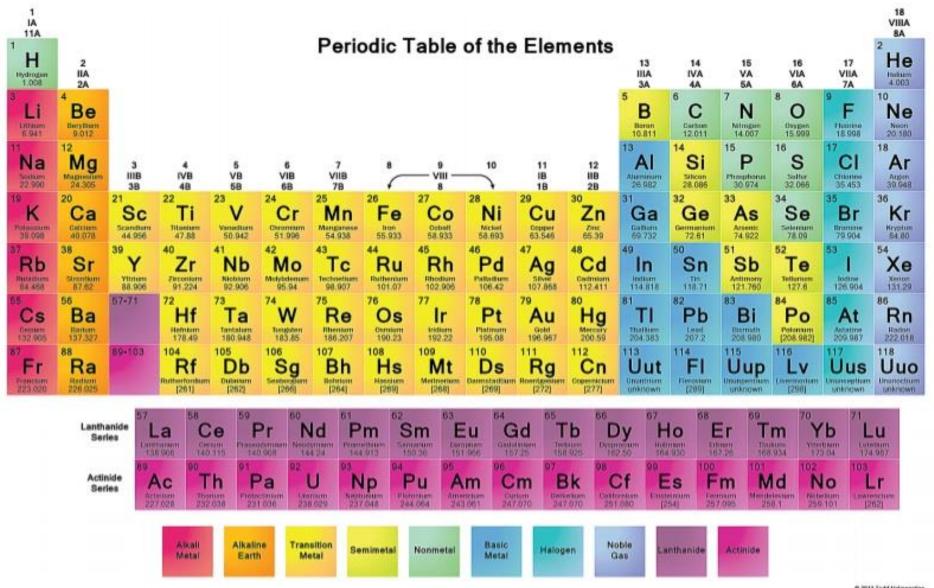
# BERKELEY MATH CIRCLE

The Math of Chemistry:

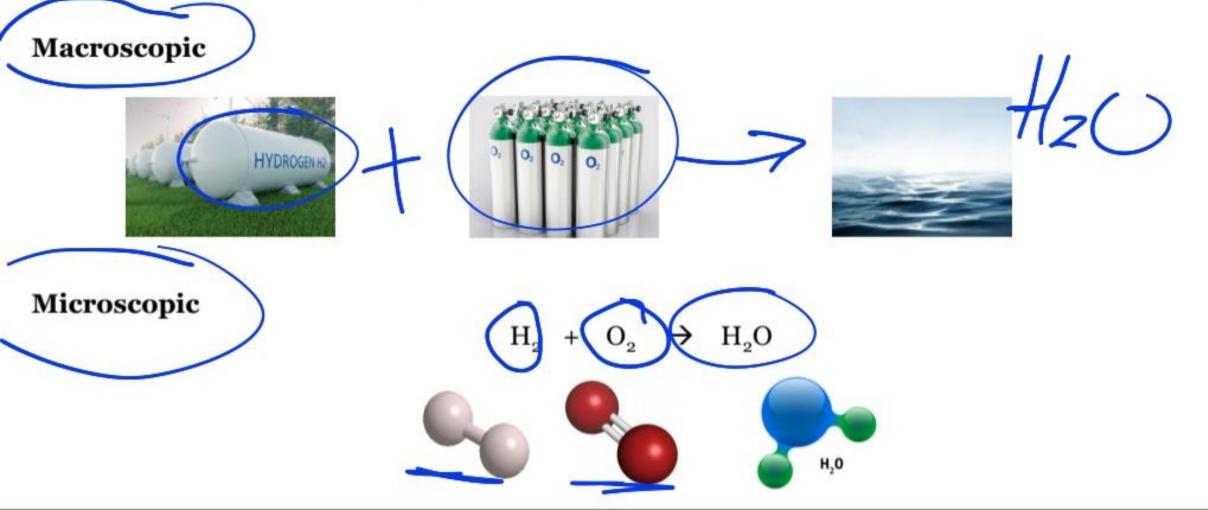
Chemical Reactions & Equilibrium

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#### The Periodic Table



In Chemistry, we like to observe reactions as they happen. The reaction is considered to be done once it reaches what we call **Equilibrium**. At Equilibrium, the macroscopic reaction is done, but we do see things occurring on the microscopic level. For example,



The reaction should continue until the reactants have been completely used up. However, this is not the case for most of the reactions because we have a **reverse reaction** taking place. Let us suppose that we begin our reaction by mixing two known reactants. At the beginning of the reaction, we have all the reactants and no products. As the reaction proceeds forward, the concentration of the reactants decreases. At the same time, the concentration of product begins to increase BUT some of the products begin to convert back to reactants.

Eventually the forward and backward reaction rates will be equal, and at this point we say that our reaction has reached dynamic chemical equilibrium.

$$H_2 + O_2 \rightleftarrows H_2O$$

We have a mathematical way to discuss this relationship, and that is referred to as the **Equilibrium Constant**, **K** (it's a fraction in essence, see below). The higher the equilibrium constant, the more products we have formed and the less reactants we have remaining. On the contrary, the smaller the equilibrium constant, the less product-favored our reaction, and the less product we have formed.

Ha + O2 = HD = Products = numerator denominator

To do some math with this concept, we need to learn some fun background science-y things. Up first is learning how to balance chemical reactions. Here goes!

## **Balancing Chemical Reactions**

The basic premise is that what goes in must come out, i.e., everything seen on the reactant side MUST also be seen on the product side. The forms of the molecules may have changed, but all the same atoms and the number of those atoms must be equal on both sides of the arrow. It's literally like an algebra equation!

For example:

We observe on the reactant side, that we have one P and five Cl's.

We see the same on the product side.

## **Balancing Chemical Reactions**

$$SO_3(g) \rightleftarrows SO_2(g) + O_2(g)$$
 (not balanced)

On the reactant side, we have one S and three O's. On the product side, we have one S and four O's.

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On the reactant side, we have two S's and six O's. We now see the same on the product side.

Let's Practice Balancing Chemical Reactions!

$$2H_{2} + O_{2} = 2H_{2}O$$
 $2H_{3} + 1O_{2} = 2H_{3}O$ 
 $2H_{3} + 1O_{2}$ 

Now that we know how to balance chemical equations, we can set-up our:

## **Equilibrium Constant (K)**

Chemical reactions can be characterized by an **equilibrium constant**, K. This constant expresses the ratio of the product of the reaction product of the reactants.

We use the concentrations (or pressures) of each molecule (those values are given or figured out per the word problem). The coefficient from the balanced chemical becomes the exponent for each term. So, for the reaction below, we have:

From our previous reactions, we would have:

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$$2H_2 + O_2 \rightleftharpoons 2H_2O \qquad \qquad = \qquad Products = \qquad (H_2O)^2 \qquad (Q_2)^2 \qquad (H_3O)^2 \qquad (H_$$

Now, let's do some math with these chemical equations:

$$2H_2 + O_2 \rightleftarrows 2H_2O$$

What is the equilibrium value for the above equation if we measured the following at equilibrium:  $\frac{1}{2}$ 

Hydrogen gas exhibits a partial pressure of 2 atm. Oxygen gas exhibits a partial pressure of 3 atm. Water vapor exhibits a partial pressure of 6 atm.

$$\frac{\text{Vater vapor exhibits a partial pressure of o athir.}}{\text{Ada }} = \frac{62}{2^2 \cdot 3} = \frac{36}{4 \cdot 3} = \frac{36}{12}$$

Using the same chemical equation,

$$2H_2 + O_2 \rightleftarrows 2H_2O$$



1) What is the water vapor's pressure at equilibrium if we seed with 4 atm of hydrogen gas and 3 atm of Oxygen gas?

What is the hydrogen's pressure at equilibrium if we started with 3 atm of water