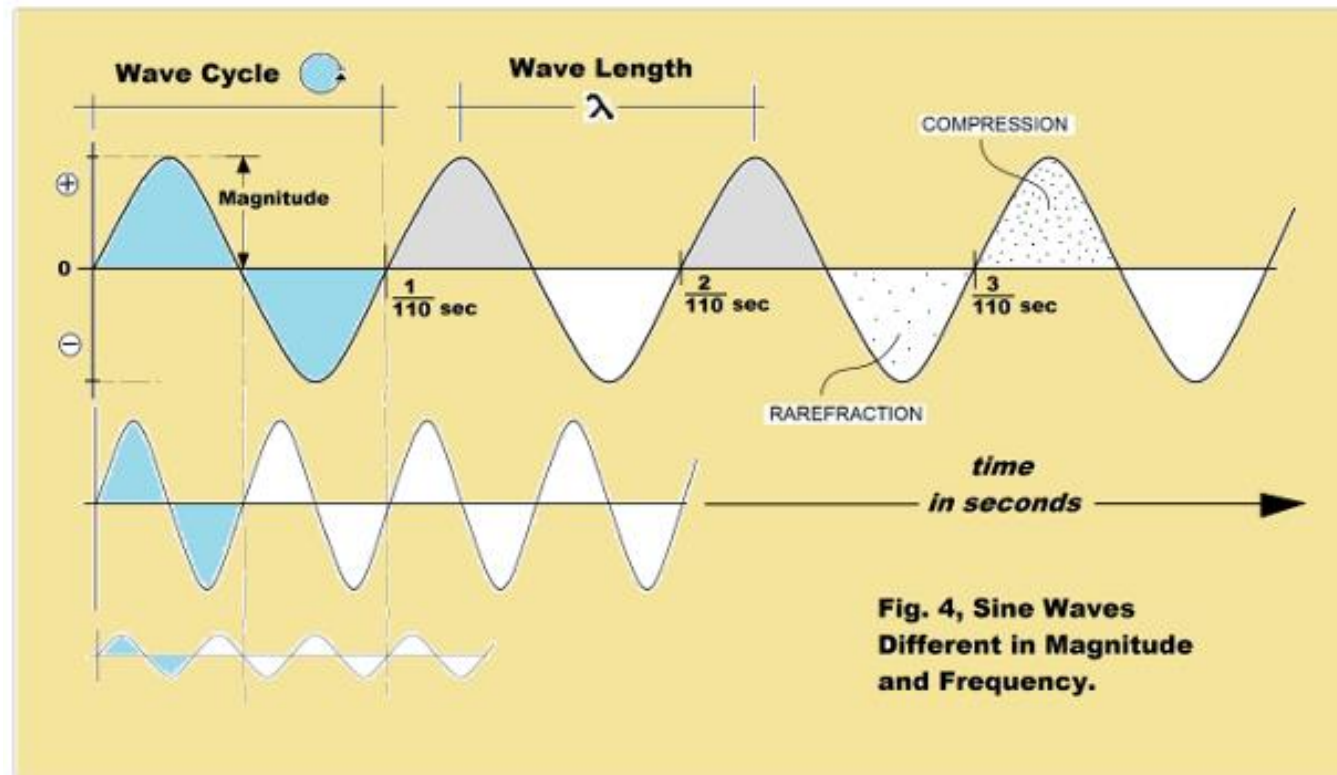


Let's transition to light and PHOTONS! We will relate this soon to Electrons ;)

Light is defined as both a WAVE and a PARTICLE!

As a PARTICLE, light exists in defined quantities known as Light Quanta or Photons, and these photons have energy associated with them (same is true for ANY moving object – think physics!). A photon is considered to be massless with no electric charge.

As a WAVE, light has properties of waves, including frequency (how often the cycle occurs) and wavelength (the length of each cycle). Mathematically, it looks like this:



Because light travels and has energy, we can calculate its energy and properties!

$$E = hf$$

E = Energy of the Photon (Joules)

h = Planck's Constant =  $6.626 \times 10^{-34}$  J-s =  **$6.6 \times 10^{-34}$  J-s**

f = frequency of photon (hertz, cycles/second = 1/s))

BUT, for waves, we can relate the frequency to the wavelength via its speed (true for any constant wave)!

Speed = frequency (f) x **wavelength ( $\lambda$ )**

(wavelength =  $\lambda$  (lambda), measured in meters)

For light then:

Speed of light = frequency (f) x wavelength ( $\lambda$ )

c = frequency (f) x wavelength ( $\lambda$ )

$$c = f \times \lambda$$

Where c = speed of light =  **$3 \times 10^8$  meters/second** – Super fast!

Therefore, combining this equation with the equation above:

$$E = hf = hc/\lambda$$

Why does this matter?

1. Properties of different light types can be studied!
2. Fun with exponent math!

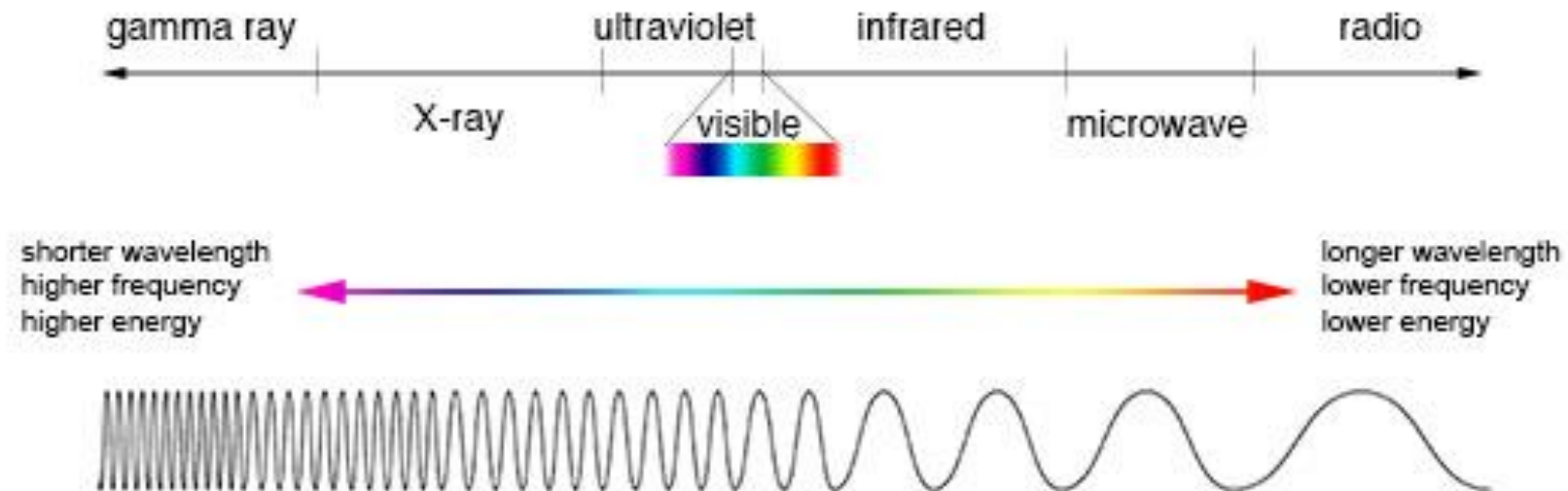
$$E = hf = hc/\lambda$$

Energy and frequency are DIRECTLY related

Energy and wavelength are INVERSELY related

↑ Energy = ↑ frequency = ↓ wavelength

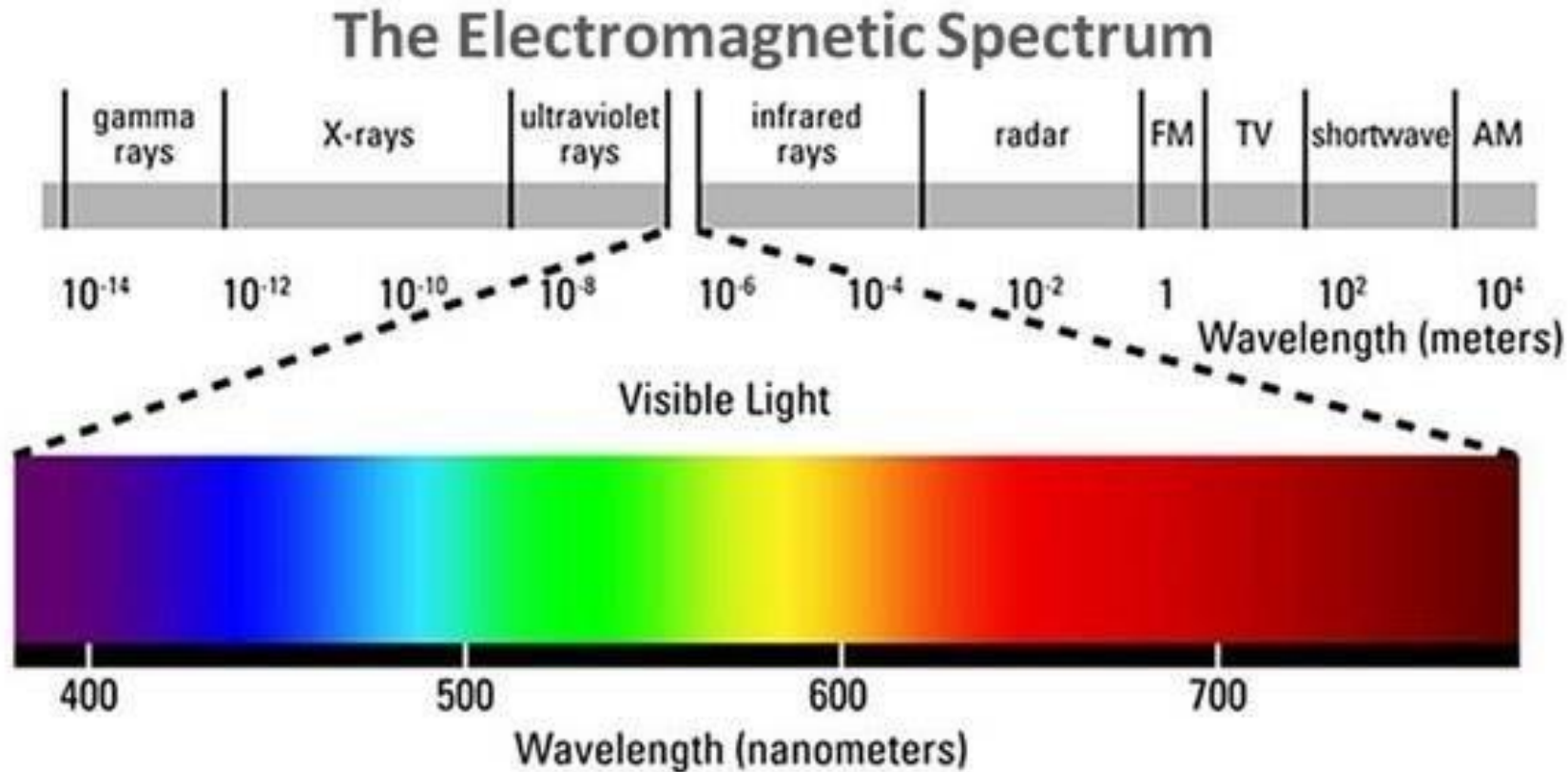
↓ Energy = ↓ frequency = ↑ wavelength



All light types have specified ranges for frequency and wavelength. Commonly, wavelength is used to describe light. The light we see, **visible light**, has wavelengths of  $4 \times 10^{-7}$  meters to  $7 \times 10^{-7}$  meters.

To measure visible light, we normally use nanometers:

1 meter =  $1 \times 10^9$  nanometers; Purple = 400 nm; Red = 700nm



## Math Problems!

## Breakout rooms!

Pick your favorite rainbow color (ROYGBV) from this chart:

Color	Wavelength	Frequency	Energy
Violet	400nm		
Blue	450nm		
Green	500nm		
Yellow	550nm		
Orange	600nm		
Red	700nm		

Calculate your favorite visible light photon's frequency and Energy.  $E = hf = hc/\lambda$

For reference:  $h = 6.6 \times 10^{-34} \text{ J}\cdot\text{s}$ ;  $c = 3 \times 10^8 \text{ m/s}$ ;  $1 \text{ m} = 1 \times 10^9 \text{ nm}$

This is a multi-step problem. Try as much mental math instead of using a calculator. Rounding off towards the final steps is acceptable ;)

## Answer (1 of 6 possibilities)!

My favorite color is Green!

**The 1<sup>st</sup> step is to convert from nanometers to meters:**

**Green = 500 nm**

$$500\text{nm} \times 1\text{m}/1 \times 10^9 \text{ nm} = 500 \times 10^0/10^9 = \mathbf{500 \times 10^{-9} = 5 \times 10^{-7} \text{ m}}$$

OR

$$500\text{nm} \times 1\text{m}/1 \times 10^9 \text{ nm} = 5 \times 10^2 \text{ nm} \times 1\text{m}/ 10^9 \text{ nm} = 5 \times 10^2 / 10^9 = \mathbf{5 \times 10^{-7} \text{ m}}$$

**The 2<sup>nd</sup> step is to use our fun, new equations!**

To give us the energy, use  $E = hc/\lambda$

$$E = hc/\lambda = (6.6 \times 10^{-34} \text{ J-s})(3 \times 10^8 \text{ m/s})/ 5 \times 10^{-7} \text{ m )}$$

$$(6.6)(3)/(5) \times (10^{-34})(10^8)/(10^{-7})$$

$$19.8/5 \times (10^{-26})/(10^{-7}) \approx 4 \times 10^{-19}$$

$$3.96 \times 10^{-19} \text{ Joules} \approx 4 \times 10^{-19} \text{ Joules}$$

## Answer (1 of 6 possibilities) Continued . . . .

Then, use your answer with this equation:  $E = hf$

$$E = hf$$

$$3.96 \times 10^{-19} \text{ Joules} = (6.6 \times 10^{-34} \text{ J-s}) \times f$$

$$f = 3.96 \times 10^{-19} / 6.6 \times 10^{-34}$$

$$f = 6 \times 10^{14}$$

Whew!

Color	Wavelength	Frequency (1/s)	Energy (J)
Violet	400nm	$7.5 \times 10^{14}$	$4.95 \times 10^{-19}$
Blue	450nm	$6.67 \times 10^{14}$	$4.4 \times 10^{-19}$
Green	500nm	$6 \times 10^{14}$	$3.96 \times 10^{-19}$
Yellow	550nm	$5.45 \times 10^{14}$	$3.6 \times 10^{-19}$
Orange	600nm	$5 \times 10^{14}$	$3.3 \times 10^{-19}$
Red	700nm	$4.29 \times 10^{14}$	$2.83 \times 10^{-19}$

Let's go back to the structure of the atom and the electron!

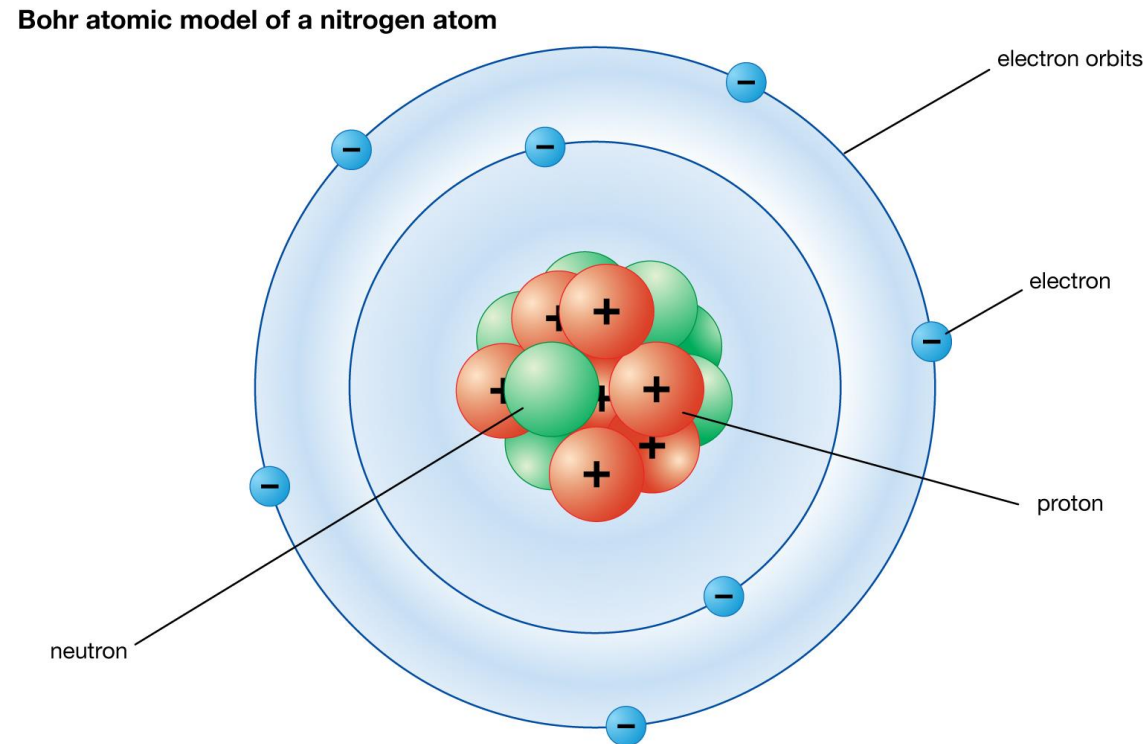
From Slide 1:

Protons & Neutron = exist in nucleus

Electron = exist outside of the nucleus

A *old* version of how to *THINK* about this is called the **Bohr Model of Atom**.

It in essence has electrons orbiting around the nucleus:



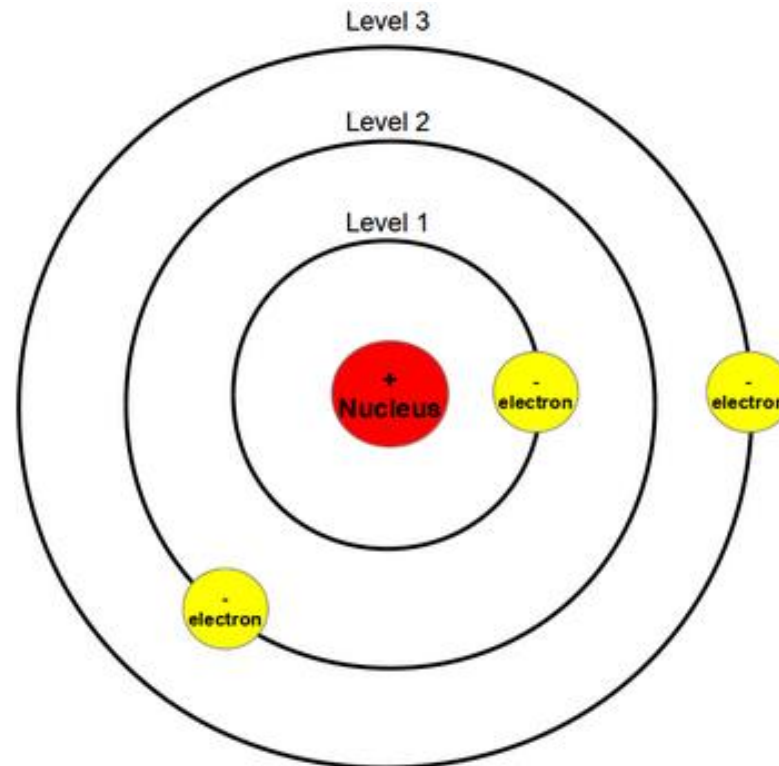


The electron orbits exist in defined energy state or levels ( $n=1$ ,  $n=2$ ,  $n=3$ , etc.).

What was discovered was that the amount of energy to go from one energy level to another is a specific amount, and this can be related to the energy of photons!

To move to higher energy level (for example,  $1 \rightarrow 3$ ), an electron **absorbs** a photon (or the energy of a photon) to get to that level.

To move to a lower energy level (for example,  $2 \rightarrow 1$ ), an electron **emits** energy in the form of a photon.

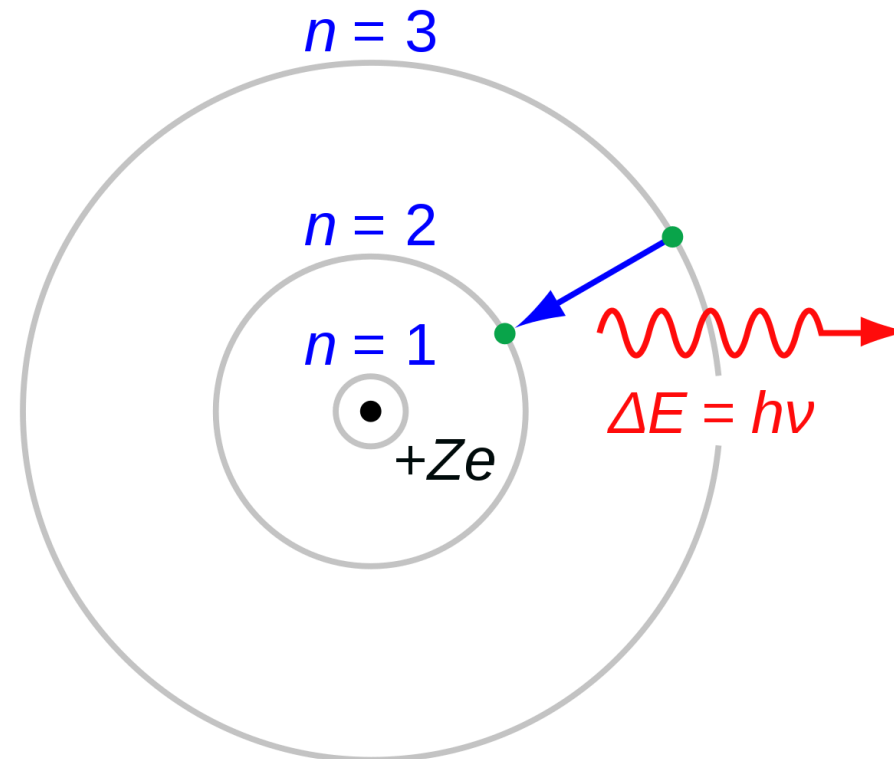


Total Energy Absorbed or Emitted is:

Energy Change = Energy of final level – Energy of initial level

With some amazing physics and math, we get to the Bohr Equation for Energy Transitions for the Hydrogen Atom:

$E = -R_E (1/n_f^2 - 1/n_i^2)$ , where  $R_E = 2.18 \times 10^{-18} \text{ J}$ , which we'll simplify to  $2 \times 10^{-18} \text{ J}$ .



## Math Problems!

$$E = -R_E (1/n_f^2 - 1/n_i^2)$$

$$R_E = 2 \times 10^{-18} \text{ J}$$

What energy is absorbed or emitted for the following transitions? No Calculators! Use fraction math and then convert to decimals when necessary

1. An electron moves from the 1<sup>st</sup> energy level to the 4<sup>th</sup> energy level.
2. An electron moves from the 4<sup>th</sup> energy level to the 2<sup>nd</sup> energy level.
3. An electron moves from the 2<sup>nd</sup> energy level to the 5<sup>th</sup> energy level.

Bonus!

1. An electron in the 1<sup>st</sup> energy leaves the atom.
2. For your answer to #2, what is the closest color of the photon emitted using our previous work? Use calculator for final step only.

Color	Wavelength	Frequency (1/s)	Energy (J)
Violet	400nm	$7.5 \times 10^{14}$	$4.95 \times 10^{-19}$
Blue	450nm	$6.67 \times 10^{14}$	$4.4 \times 10^{-19}$
Green	500nm	$6 \times 10^{14}$	$3.96 \times 10^{-19}$
Yellow	550nm	$5.45 \times 10^{14}$	$3.6 \times 10^{-19}$
Orange	600nm	$5 \times 10^{14}$	$3.3 \times 10^{-19}$
Red	700nm	$4.29 \times 10^{14}$	$2.83 \times 10^{-19}$

## Answers!

$$E = -R_E (1/n_f^2 - 1/n_i^2)$$

$$R_E = 2 \times 10^{-18} \text{ J}$$

What energy is absorbed or emitted for the following transitions?

1. An electron moves from the 1<sup>st</sup> energy level to the 4<sup>th</sup> energy level.

$$E = -R_E (1/n_f^2 - 1/n_i^2) = (-2 \times 10^{-18}) (1/4^2 - 1/1^2) = (-2 \times 10^{-18}) (1/16 - 1/1) = (-2 \times 10^{-18}) (1/16 - 16/16) = (-2 \times 10^{-18}) (-15/16) = (2)(15/16)(10^{-18}) = (15/8)(10^{-18}) = \mathbf{1.875 \times 10^{-18} \text{ J Absorbed}}$$

2. An electron moves from the 4<sup>th</sup> energy level to the 2<sup>nd</sup> energy level.

$$E = -R_E (1/n_f^2 - 1/n_i^2) = (-2 \times 10^{-18}) (1/2^2 - 1/4^2) = (-2 \times 10^{-18}) (1/4 - 1/16) = (-2 \times 10^{-18}) (4/16 - 1/16) = (-2 \times 10^{-18}) (3/16) = (-2)(3/16)(10^{-18}) = (-3/8)(10^{-18}) = \mathbf{-0.375 \times 10^{-18} \text{ J Emitted}}$$

3. An electron moves from the 2<sup>nd</sup> energy level to the 5<sup>th</sup> energy level.

$$E = -R_E (1/n_f^2 - 1/n_i^2) = (-2 \times 10^{-18}) (1/5^2 - 1/2^2) = (-2 \times 10^{-18}) (1/25 - 1/4) = (-2 \times 10^{-18}) (4/100 - 25/100) = (-2 \times 10^{-18}) (-21/100) = (2)(21/100)(10^{-18}) = (42/100)(10^{-18}) = \mathbf{0.42 \times 10^{-18} \text{ J Absorbed}}$$

## Answers . . . . Bonus!

$$E = -R_E (1/n_f^2 - 1/n_i^2); R_E = 2 \times 10^{-18} \text{ J}$$

1. An electron in the 1<sup>st</sup> energy leaves the atom.

$$n_f = \text{infinity!} = \infty$$

$$n_i = 1$$

$$E = -R_E (1/\infty^2 - 1/n_i^2) = (-2 \times 10^{-18}) (1/\infty^2 - 1/1^2) = (-2 \times 10^{-18}) (0 - 1/1) = (-2 \times 10^{-18}) (-1) = \mathbf{2 \times 10^{-18} \text{ J Absorbed}}$$

2. For your answer to #2, what is the closest color of the photon emitted using our previous work?

$$\text{Photon Energy} = -0.375 \times 10^{-18}$$

And we know  $E = hf$

$$0.375 \times 10^{-18} = (6.6 \times 10^{-34})f$$

$$f = 0.375 \times 10^{-18} / 6.6 \times 10^{-34} = \frac{3}{8} \times 10^{-18} / 6 \frac{3}{5} \times 10^{-34} = \left(\frac{3}{8} / 6 \frac{3}{5}\right) (10^{-18} / 10^{-34}) = \left(\frac{3}{8} / \frac{33}{5}\right) (10^{16}) = \left(\frac{3}{8} \times \frac{5}{33}\right) (10^{16}) = \left(\frac{1}{8} \times \frac{5}{11}\right) (10^{16}) = \left(\frac{5}{88}\right) (10^{16}) = 0.057 \times 10^{16} = 5.7 \times 10^{14} \rightarrow \text{in between Yellow/Green}$$

Color	Wavelength	Frequency (1/s)	Energy (J)
Violet	400nm	$7.5 \times 10^{14}$	$4.95 \times 10^{-19}$
Blue	450nm	$6.67 \times 10^{14}$	$4.4 \times 10^{-19}$
Green	500nm	$6 \times 10^{14}$	$3.96 \times 10^{-19}$
Yellow	550nm	$5.45 \times 10^{14}$	$3.6 \times 10^{-19}$
Orange	600nm	$5 \times 10^{14}$	$3.3 \times 10^{-19}$
Red	700nm	$4.29 \times 10^{14}$	$2.83 \times 10^{-19}$