
BERKELEY MATH CIRCLE

Information, Number Systems, and Computers

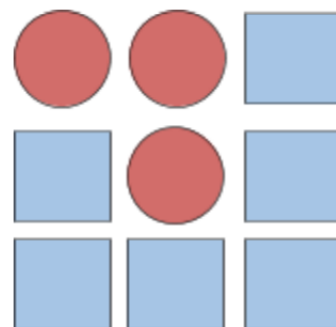
December 2020

Circle-Square Patterns

Challenge 1: Patterns

Record all of the possible three place value patterns that use only the circle and square shapes. A few are listed in the diagram to the right.

Try to make sure these patterns are in some type of order and avoid putting down patterns randomly



1) _____

2) _____

3) _____

4) _____

5) _____

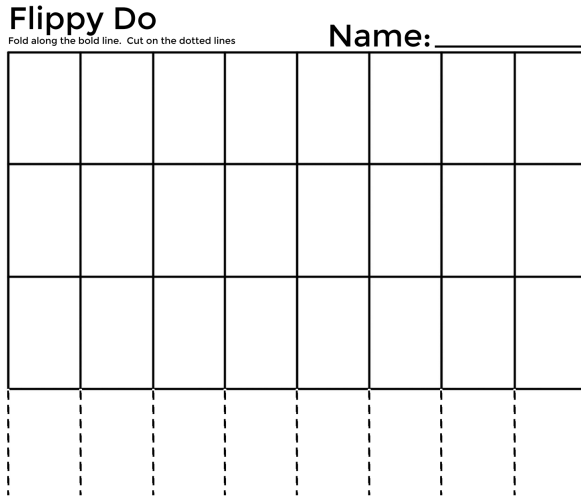
6) _____

7) _____

8) _____

Flippy-Do

On a separate sheet of paper, draw 7 vertical lines (folding in half three times, "hamburger style") and 3 horizontal lines (folding in half twice "hotdog style") to make your flippy do. It should look something like this graphic below.



Use your flippy-do to answer the following questions.

All 4-Bit Numbers: Fill in the binary equivalents for the decimal numbers below. We've started the first three for you.

Binary: 4-bit number	Decimal
0000	0
0001	1
0010	2

Binary: 4-bit number	Decimal

What do you notice when you compare the odd numbers with the even numbers?
 What might explain this?

Binary Numbers with exactly one 1: Complete the chart with all 8-bit binary numbers that have exactly one 1. We've done the first two for you.

Binary: 8-bit number (with exactly one 1)	Decimal
0000 0001	1
0000 0010	2
0000 0100	

Binary: 8-bit number (with exactly one 1)	Decimal

What do you notice about the decimal equivalents above?

Conversion Practice: Find the equivalent binary or decimal numbers below.

Binary	Decimal
100	
101	
1101	
0001 1111	
0010 0000	
1010 1010	
1111 1111	

Binary	Decimal
	5
	17
	63
	64
	127
	256
	513

When you add a zero to the right of a decimal number, it multiplies its value by 10 (For example, 15 becomes 150). What similar result happens to the value of a binary number when you add a zero on the right? (For example, 11 would become 110).

Do the binary numbers 0011 and 000011 have the same value or different values? Explain.

Would two bits be enough to assign a unique binary number to each vowel in the English language? Explain.

How many bits would you need if you wanted to count up to the decimal number 1000?